NAME

qglqrc − Gauss-Laguerre logarithmic Quadrature Recursion Coefficients

SYNOPSIS

Fortran (77, 90, 95, HPF):

f77 *[flags] file(s) . . . -L/usr/local/lib -lgjl*

```
SUBROUTINE qglqrc (a, b, s, t, alpha, nquad, ierr)
INTEGER        ierr,     nquad
REAL*16        a(0:MAXPTS), alpha,     b(0:MAXPTS)
REAL*16        s(0:MAXPTS), t(0:MAXPTS)
```

C (K&R, 89, 99), C++ (98):

cc *[flags] -I/usr/local/include file(s) . . . -L/usr/local/lib -lgjl*

Use

#include <gjl.h>

to get this prototype:

```
void qglqrc(fortran_quadruple_precision a_[],
        fortran_quadruple_precision b_[],
        fortran_quadruple_precision s_[],
        fortran_quadruple_precision t_[],
        const fortran_quadruple_precision * alpha_,
        const fortran_integer * nquad_,
        fortran_integer * ierr_);
```

NB: The definition of C/C++ data types **fortran_** *xxx*, and the mapping of Fortran external names to C/C++ external names, is handled by the C/C++ header file. That way, the same function or subroutine name can be used in C, C++, and Fortran code, independent of compiler conventions for mangling of external names in these programming languages.

DESCRIPTION

Compute the recursion coefficients and zeroth and first moments of the monic polynomials corresponding to the positive weight function

w(x,\alpha) = (x − 1 − ln(x)) * exp(−x) * x^\alpha

with recursion relation (n = 0, 1, 2, . . .)

P_{n+1}^\alpha(x) = (x − B_n^\alpha) * P_n^\alpha(x)
    − A_n^\alpha * P_{n−1}^\alpha(x)

and initial conditions

P_{−1}^\alpha(x) = 0
P_{0}^\alpha(x) = 1

Except in the weight function, the superscripts indicate dependence on \alpha, NOT exponentiation.

The required moments are:

T_n^\alpha = \int_0^\infty w(x,\alpha) (P_n^\alpha(x))^2 dx
S_n^\alpha = \int_0^\infty w(x,\alpha) (P_n^\alpha(x))^2 x dx

From these moments, the recursion coefficents are computed as:

A_n^\alpha = T_n^\alpha / T_{n−1}^\alpha
B_n^\alpha = S_n^\alpha / T_n^\alpha

On entry:

alpha Power of x in the integrand (**alpha** > −1).

nquad Number of quadrature points to compute. It must be less than the limit MAXPTS defined in the header file, *maxpts.inc.* The default value chosen there should be large enough for any realistic application.

On return:

a(0. .**nquad**)	Recursion coefficients: **a**(n) = A_n^\alpha.
b(0. .**nquad**)	Recursion coefficients: **b**(n) = B_n^\alpha.
s(0. .**nquad**)	First moments: **s**(n) = S_n^\alpha
t(0. .**nquad**)	Zeroth moments: **t**(n) = T_n^\alpha
ierr	Error indicator: = 0 (success), 1 (eigensolution could not be obtained), 2 (destructive overflow), 3 (**nquad** out of range), 4 (**alpha** out of range).

SEE ALSO

qglqf(3), **qglqfd**(3).

AUTHORS

The algorithms and code are described in detail in the paper

Fast Gaussian Quadrature for Two Classes of Logarithmic Weight Functions

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